# Doping dependence of the superconducting transition temperature in electron-doped $\mathrm{SrTiO}_{3}$ based on the firstprinciples calculations 

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$\mathrm{SrTiO}_{3}$ is a wide-gap semiconductor with a bandgap of 3.2 eV . When $n$-type carriers (electrons) are introduced in $\mathrm{SrTiO}_{3}$ through oxygen reduction[1] or Nb -doping[2], the superconductivity is observed for a wide range of low carrier concentrations $n=10^{18} \sim 10^{21} / \mathrm{cm}^{3}$ where the transition temperature $T_{\mathrm{c}}$ shows a characteristic dome shape as a function of $n$ with a peak of $T_{\mathrm{c}}=0.45 \mathrm{~K}$ at $n \sim 10^{20} / \mathrm{cm}^{3}$. In addition, a recent experiment for further low carrier concentrations down to $10^{17} / \mathrm{cm}^{3}$ has revealed that $T_{\mathrm{c}}$ shows another dome shape with a peak of $T_{\mathrm{c}}=0.21 \mathrm{~K}$ at $n \sim 10^{18} / \mathrm{cm}^{3}[3]$ where the number of energy bands across the Fermi level changes from two to one with decreasing $n$. Theoretically, the $T_{\mathrm{c}}$ dome for $n=10^{18} \sim 10^{21} / \mathrm{cm}^{3}$ was well accounted for by the plasmon mechanism of superconductivity with taking into account of the polar optical phonons responsible for the ferroelectric behavior of this system[4]. The details of the energy band dispersions as well as the phonon dispersions, however, have not been explicitly considered there. In the present paper, we investigate the electronic and phonon states of electron-doped $\mathrm{SrTiO}_{3}$ on the basis of the first-principles calculations and discuss the doping dependence of $T_{c}$ by using the McMillan equation where the effect of the plasmon is included in the effective Coulomb pseudopotential $\mu^{*}$ as recently developed for various doped semiconductors[5,6].
[1] J. F. Schooley et al., Phys. Rev. Lett. 14, 305 (1965).
[2] E. R. Pfeiffera and J. F. Schooley, Phys. Lett. A 29, 589 (1969).
[2] X. Lin et al., Phys. Rev. Lett. 112, 207002 (2014).
[4] Y. Takada, J. Phys. Soc. Jpn. 49, 1267 (1980).
[5] K. Sano, M. Seo and K. Nakamura, J. Phys. Soc. Jpn. 88, 093703 (2019).
[6] K. Sano, Y. Nitta and Y. Ōno, J. Phys. Soc. Jpn. 89, 113704 (2020).

